

# Tutorium to Introduction to AI, 3rd week - Nicolas Höning

Nicolas Höning

April 28, 2006

## organizational issues

### some random tips and tricks

built-in predicates are not for free  
base cases: "once" vs "every time"

### Gauss reconsidered

the fruits of left recursion  
accumulators

## organizational issues

- ▶ sorry for the late homework results. we're having some technical problems...  
almost all of them were really fine, so don't worry :-)  
we need to get all of you in groups, so what about these people:  
Anna-Antonia Pape, Benjamin Wulff, Janine Yvonne Willbrand, Da Sheng Zhang, Annett Wegner, Gunther Baumgartner, Arthur Legler, Jonas Volger, Yvonne Eberl, Johannes Emden

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- ▶ we also found out yesterday that the Prolog system on VIPS didn't always show all error messages :-)

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So if there is anything you want to talk about or that should be done differently, don't hesitate to tell me.
- ▶ that also includes repetitions. if we need to reconsider some basic concepts in order for you to really get them, then that is really worth the time. Ask me!

## built-in predicates are not for free

- ▶ this week's homework suggests to have a look at the manual to find a built-in predicate that appends a list to another list (it's uploaded in Stud.IP and called "learn\_prolog.pdf" and it's really readable. check it out.)

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- ▶ you should especially read chapter 6. It might help with that exercise, but mostly it helps to really grasp that damn recursion thing.



## built-in predicates are not for free

- ▶ you would also learn that `append` is inefficient, because it always works up and down the same list. As we will later deal with efficiency a lot, this is good to understand right at the beginning.  
Average programmers think of using a library function as one call, good programmers care about the implementation of that library function.

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Average programmers think of using a library function as one call, good programmers care about the implementation of that library function.
- ▶ if you have time on the bus, read [this brilliant essay by Joel Spolsky](#) about that topic (not Prolog-related, but a good read).

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- ▶ the base case can be the distinction between "once" and "every time"

## last weeks Gauss: the limitations

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$$\sum_{i=0}^x i = \frac{x}{2}(x + 1)$$

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`gauss(0,0).`  
`gauss(X,Y) :-`  
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- ▶ it needed both X and Y instantiated. Why?
- ▶ When you do not know X, and of course you don't yet know X1, the term `X1isX - 1` has infinitely many solutions. The same holds for `Y1isY - X`

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- ▶ so last week's Gauss was  $gauss(+X, +Y)$
- ▶ let's think about  $gauss(+X, -Y)$  now



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- ▶ How can we decrement X to zero, from the first call down to the base case, while we add all those Xes up to Y, beginning at the base case?

## left recursion: a simple example

- ▶ ok, take a break, look at this simple predicate here:  
recurse([]).  
recurse([H|Rest]) :-  
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Twice.
- ▶ Once in right-recursion-style and once in left-recursion-style.  
Now what will be the output of `recurse([a,b,c,d]).?`

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down the recursion tree and up again.



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- ▶ we see the way to the base case, and then we see the way back from it.  
down the recursion tree and up again.
- ▶ Now, right recursion is the usual way to go, but left recursion seems to make sense for some problems...

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- ▶ ok, we should change our gauss example, but just a little:

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/* gauss_with_X(+X,-Y) */  
gauss_with_X(X,-) :- X < 0, !, fail.  
gauss_with_X(0,0).  
gauss_with_X(X,Y) :-  
    X1 is X - 1,  
    gauss_with_X(X1,Y1),  
    Y is Y1 + X.
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- ▶ the only changes are switching the last two lines, so we compute Y in left recursion (after it has been instantiated to zero by the base case), and using addition to compute Y instead of subtraction.

# $\text{gauss}(-X,+Y)$

- ▶ ok, now what about  $\text{gauss}(-X,+Y)$ ? Can we do it the same way?

## gauss(-X,+Y)

- ▶ ok, now what about *gauss(-X,+Y)*? Can we do it the same way?
- ▶ the problem is: we cannot decrement Y just as easy as X. X was decremented by one, Y would be decremented by an X we don't yet know.

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- ▶ ok, now what about  $\text{gauss}(-X,+Y)$ ? Can we do it the same way?
- ▶ the problem is: we cannot decrement  $Y$  just as easy as  $X$ .  $X$  was decremented by one,  $Y$  would be decremented by an  $X$  we don't yet know.
- ▶ I'll use another interesting technique to solve that one: the accumulator.

## accumulators: why?

- ▶ ok, the problem again: if we have  $Y$  but no  $X$ , we cannot decrement  $Y$  till we reach zero, because we don't know by what we should decrement. We only have an  $X$  parameter that should hold the  $X$  we are looking for but is not instantiated



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- ▶ well... we could instantiate  $X$  with zero and increment it by one with every step. Then we could decrement  $Y$  by that  $X$  and if it comes down to zero, we incremented  $X$  up to the one we were looking for!

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- ▶ But if we instantiate  $X$  with zero in the first place, we will never get to see that incremented  $X$  that comes up in the base case :-)
- ▶ so how about introducing another dummy parameter?

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- ▶ an accumulator is a name for another technique while using recursion.  
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- ▶ there the parameter we want to instantiate with the solution (here: X) is instantiated with the accumulator, passed up the recursion tree, and we're done.
- ▶ This technique does no harm to the efficiency of your program (you'll find it again in that chapter 6 I talked about earlier).

## gauss(-X,+Y)

- ▶ ok, let's do this: Z is our accumulator:  
gauss\_with\_Y\_2(.,Y,.) :- Y < 0, !, fail.  
gauss\_with\_Y\_2(X,0,X).  
gauss\_with\_Y\_2(X,Y,Z) :-  
    Z1 is Z + 1,  
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- ▶ we'll add it up from zero to the value that X should have.  
Then we unify it with X and pass X up the recursion tree
- ▶ we're back to good old right recursion again

## gauss(-X,+Y): cleaning up

- ▶ ok, the user probably doesn't want to call *gauss\_with\_Y2(X,5050,0)*.

## gauss(-X,+Y): cleaning up

- ▶ ok, the user probably doesn't want to call *gauss\_with\_Y2(X,5050,0)*.
- ▶ `/* gauss_with_Y(-X,+Y)`  
this pipes the problem to our  
special accumulator predicate `*/`  
`gauss_with_Y(X,Y) :-`  
`gauss_with_Y_2(X,Y,0).`

## gauss(X,Y): cleaning up

- ▶ and now we let the user call `gauss(X,Y)` and find out ourselves if X is in there or Y is:

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- ▶ and now we let the user call `gauss(X,Y)` and find out ourselves if X is in there or Y is:
- ▶ `gauss(X,Y) :-`  
    `number(X),`  
    `gauss_with_X(X,Y).`
- `gauss(X,Y) :-`  
    `number(Y),`  
    `gauss_with_Y(X,Y).`

the end

▶ questions?